

# Single Sideband and Ring Modulator

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# Normal AM

- The AM modulated signal is given by:

$$s(t) = A_c (1 + k_a m(t)) \cos 2\pi f_c t$$

- Low power efficiency of the normal AM signal. Most of the transmitted power is allocated to the carrier frequency, which does not carry information.
- Information resides in the sidebands.

# DSB-SC:

- In a DSB-SC, there is no transmitted carrier.
- All power is allocated to the two sidebands.
- The transmission bandwidth is twice the message bandwidth.
- Information about the message is contained both in the upper and lower sidebands.

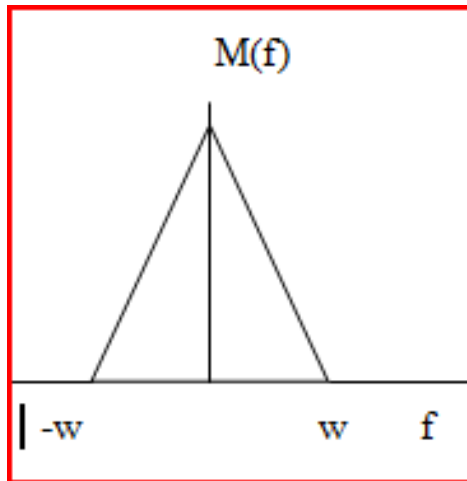
$$s(t) = A_c m(t) \cos 2\pi f_c t$$

# DSB-SC Modulation and Demodulation

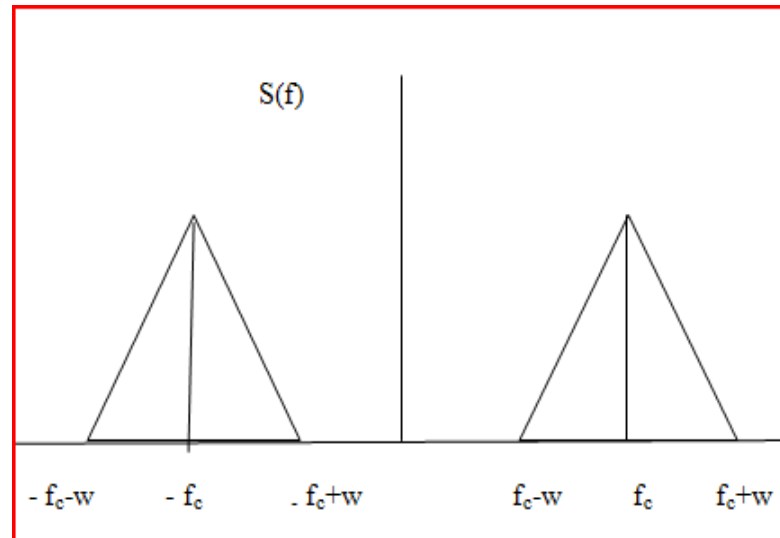
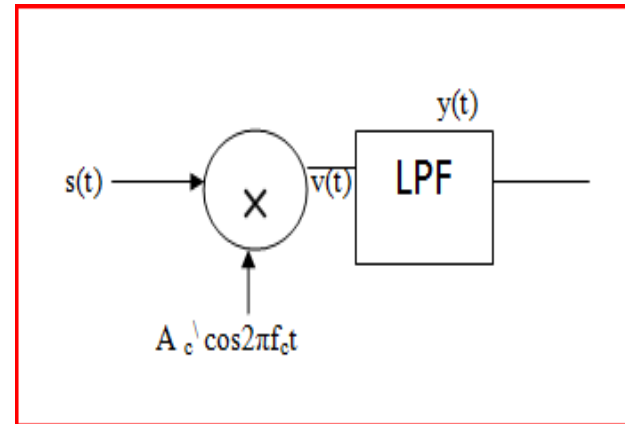
## Modulation

$$s(t) = A_c m(t) \cos 2\pi f_c t$$

The ring modulator is used to perform modulation. Its operation will be explained later.



Coherent Demodulation is used to recover the message



# Single Sideband Modulation

- The information represented by the modulating signal is contained in both the upper and the lower sidebands.
- It is not necessary to transmit both side-bands. Either one can be suppressed at the transmitter without any information lost
- In SSB-SC the carrier is suppressed and one of the two sideband is transmitted
- Hence, **power saving** and **bandwidth saving**
- Sometimes, an attenuated part of the carrier is transmitted that will ease the process of demodulation.

# Single Sideband Modulation

- The SSB modulated signal is represented in the time domain as:

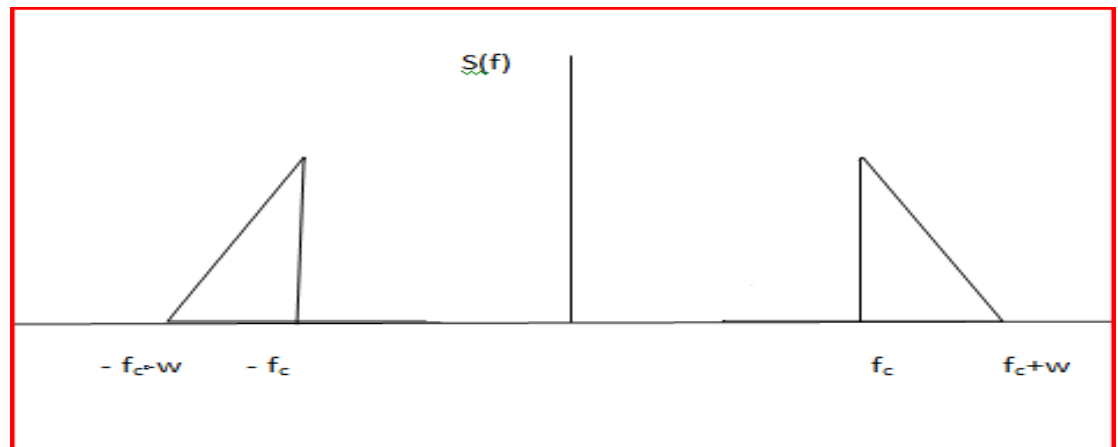
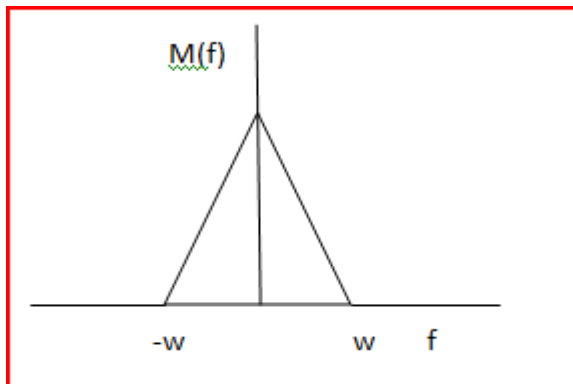
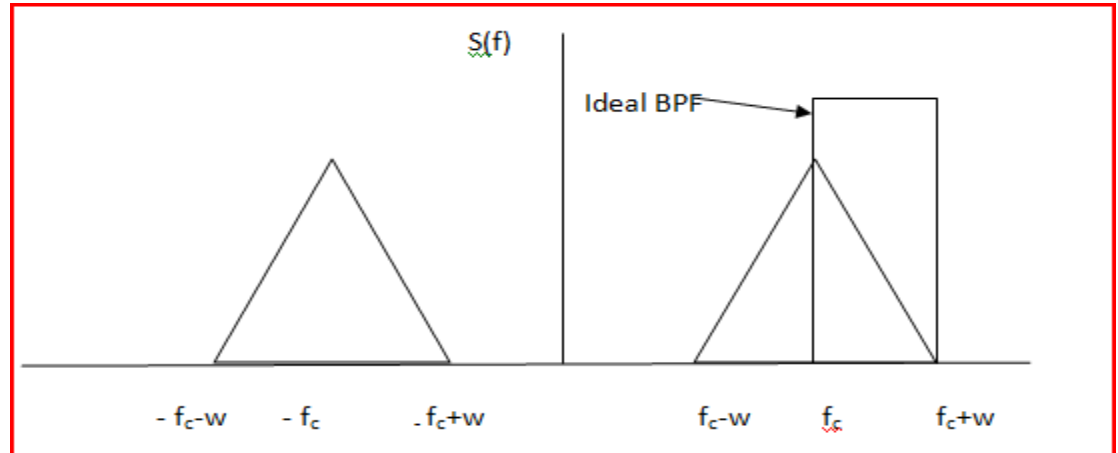
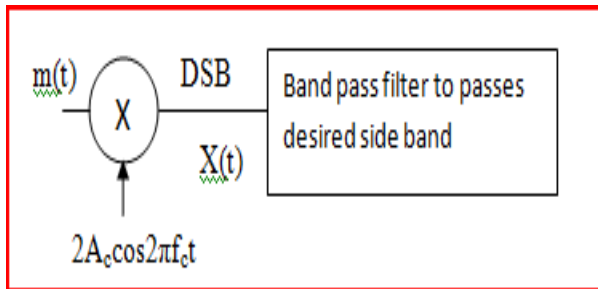
$$s(t) = A_c m(t) \cos 2\pi f_c t - A_c \hat{m}(t) \sin 2\pi f_c t$$

*Here,  $\hat{m}(t)$  is the Hilbert transform of  $m(t)$  and is obtained by passing  $m(t)$  through a 90 degrees phase shifter.*

# Generating a SSB signal

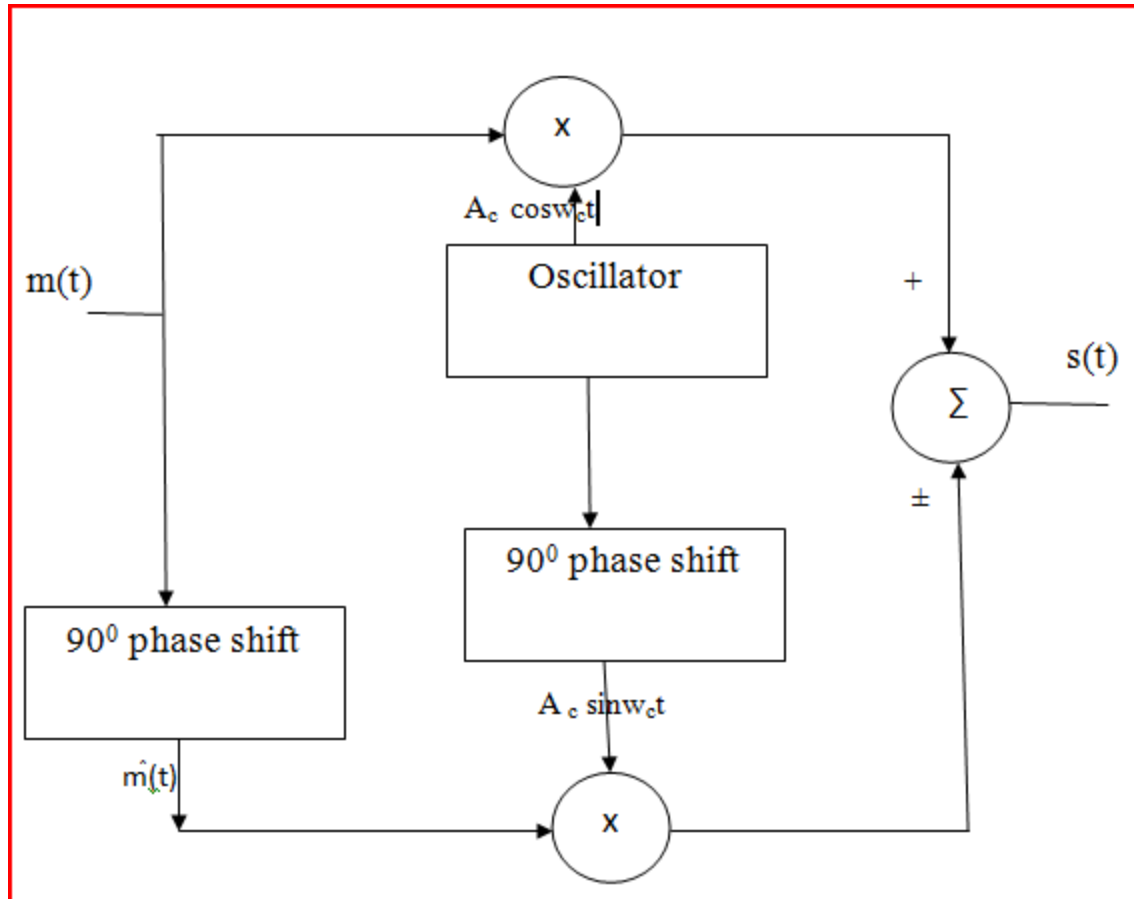
- **The Frequency discrimination method** (Filtering Method) is used in this experiment to generate the SSB signal.
- Here, A DSB-SC carrier signal is generated first, and then the desired sideband is selected using the appropriate bandpass filter.
- Another method for generating the SSB signal is called the **phasing method**: The SSB can be generated means of two DSB-SC modulators that are out of phase by 90 degrees.

# Generating a SSB signal

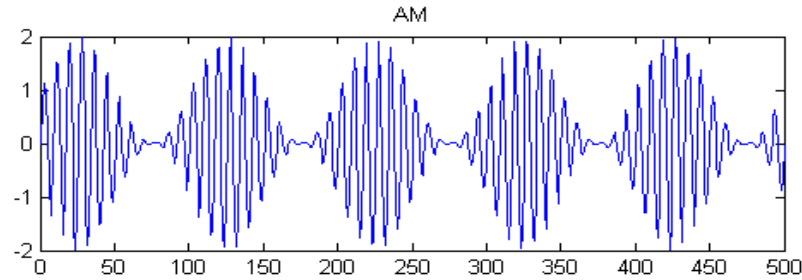




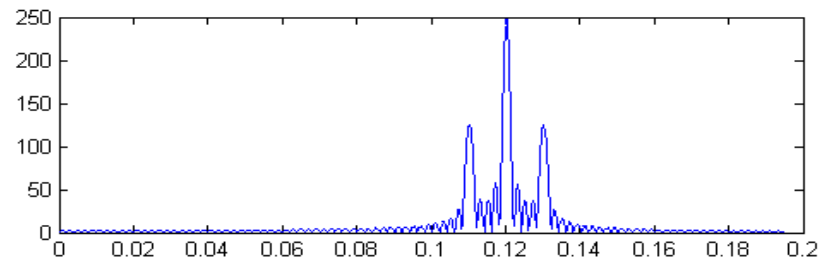
# SSB Generation: Phasing Method



$$\begin{aligned} \text{(DSB-SC)I} &= \cos 2\pi(fc - fm)t + \cos 2\pi(fc + fm)t \\ \text{(DSB-SC)Q} &= \cos 2\pi(fc - fm)t - \cos 2\pi(fc + fm)t \end{aligned}$$

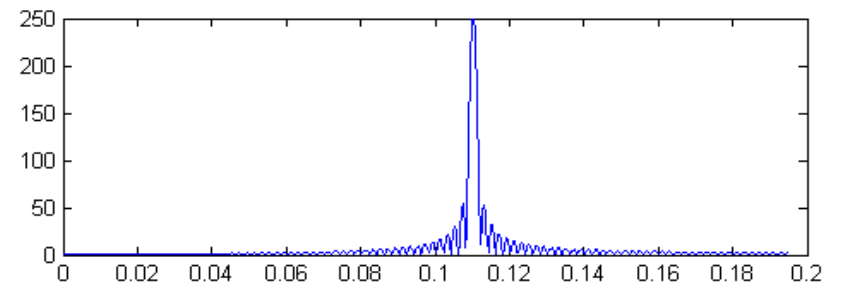
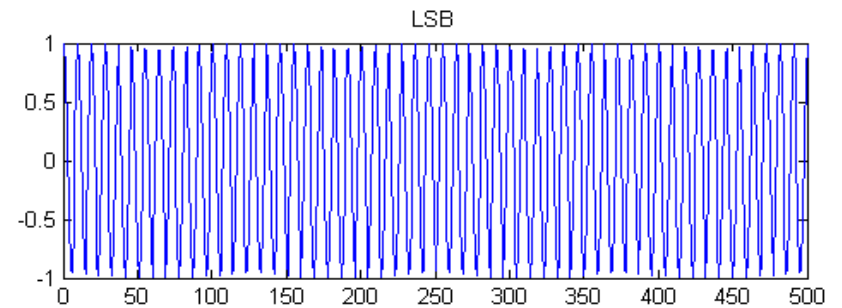
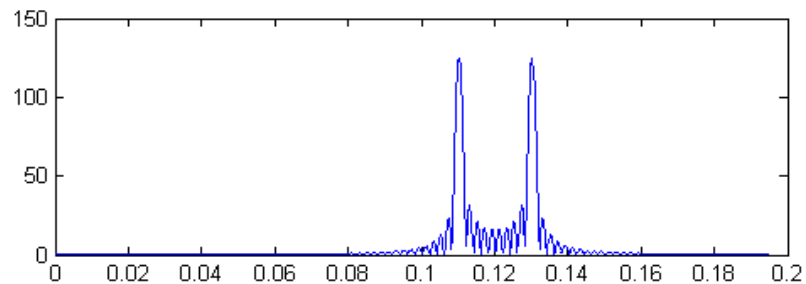
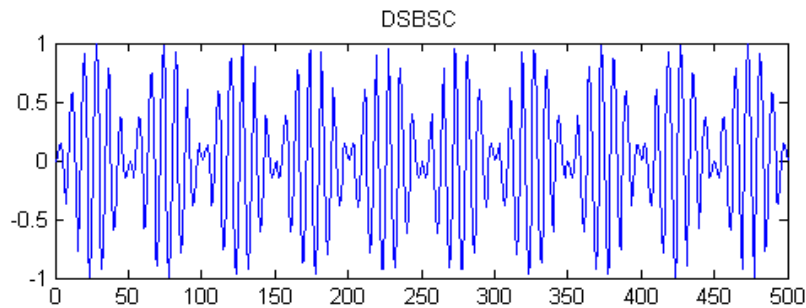


AM in time and frequency domains



SSB in time and frequency domains

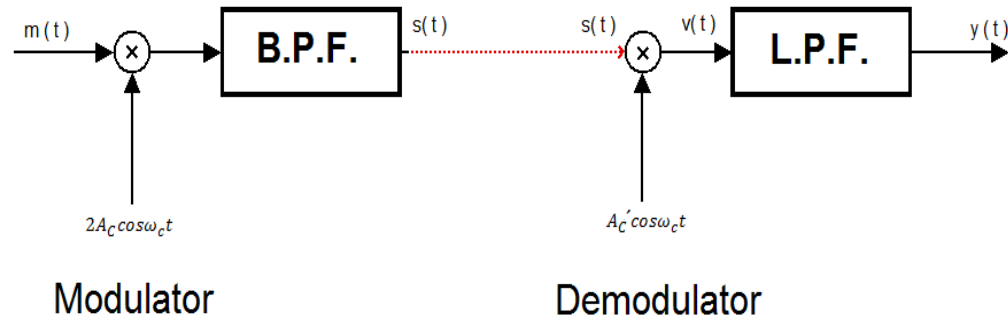
DSB in time and frequency domains



# SSB Demodulation

- Coherent Demodulation is used to retrieve the baseband message signal
- A coherent detector uses the knowledge of the phase and frequency of the carrier wave to demodulate the signal.
- It is simply a product device, which multiplies the SSB signal by a sinusoidal signal having the same frequency as the transmitted carrier, followed by a low pass filter ( LPF).

# SSB Coherent Demodulation



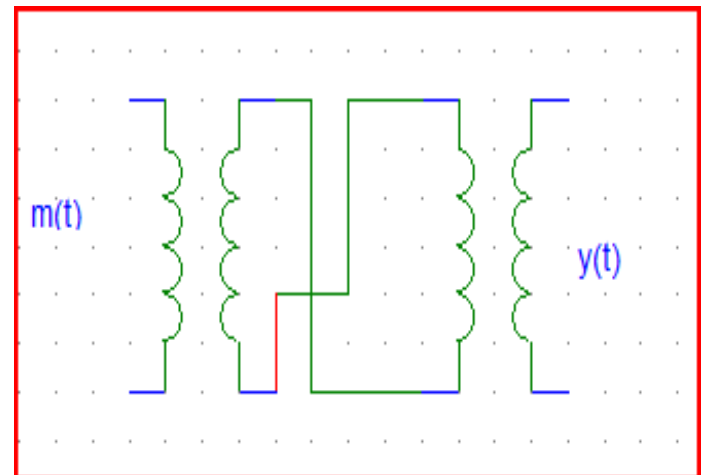
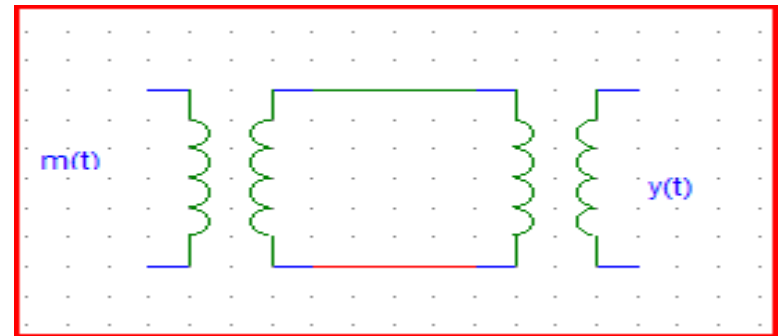
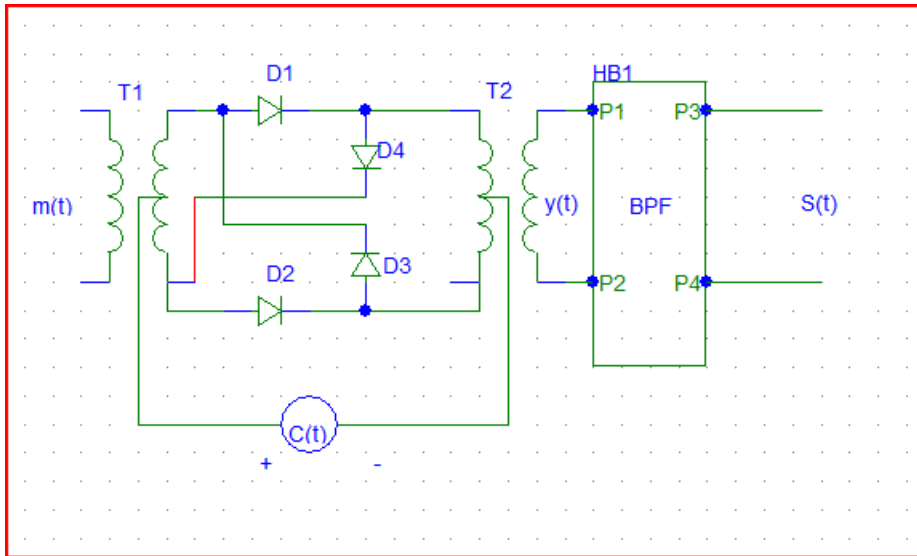
$$\begin{aligned}
 v(t) &= s(t)A_c' \cos \omega_c t \\
 &= A_c' [A_c m(t) \cos \omega_c t - A_c \hat{m}(t) \sin \omega_c t] \cos \omega_c t \\
 &= A_c A_c' m(t) \cos 2\omega_c t - A_c A_c' \hat{m}(t) \sin \omega_c t \cos \omega_c t \\
 &= \frac{A_c A_c'}{2} m(t) + \frac{A_c A_c'}{2} m(t) \cos 2\omega_c t - \frac{A_c A_c'}{2} \hat{m}(t) \sin 2\omega_c t
 \end{aligned}$$

The low pass filter admits only the first terms. The output is:

$$y(t) = \frac{A_c A_c'}{2} m(t)$$

# Ring Modulator

Used for the generation of a DSB signal. It consists of a ring of 4 diodes and two transformers.



# Ring Modulator

- During +ve half cycle of the carrier, message multiplied by +1
- During – ve half cycle, it is multiplied by -1.
- Net effect, as if message is multiplied by a square function.

$$y(t) = m(t)\left[\frac{4}{\pi} \cos 2\pi f_c t - \frac{4}{3\pi} \cos 3(2\pi f_c t) + \frac{4}{5\pi} \cos 5(2\pi f_c t)\right]$$
$$= m(t)\frac{4}{\pi} \cos 2\pi f_c t - m(t)\frac{4}{3\pi} \cos 3(2\pi f_c t) + m(t)\frac{4}{5\pi} \cos 5(2\pi f_c t)$$

When  $y(t)$  passes through the BPF, the only component that appears at the output is the desired DSB-SC signal, which is

$$s(t) = m(t)\frac{4}{\pi} \cos 2\pi f_c t$$

# Ring Modulator

- Net operation of the ring modulator can be modeled as multiplying the message by a periodic square function.

